

# Design of a Hybrid Interest-Based Peer-to-Peer Network Using Residue Class-based Topology and Star Topology

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## Abstract

## 1 Introduction

In this work, a hybrid interest-based peer-to-peer network is presented. It consists of the existing Residue-class (RC) based peer-to-peer (P2P) network and the Star interconnection network. The former one has been considered because of its two main advantages viz. (1) all peers with the same interest (or possessing same resource type) structurally form a group of diameter one, and (2) the group heads are connected in the form of a ring and the ring always remains connected even in presence of any churn. The Star topology has been considered because of its low diameter. We have incorporated these above advantages of the two architectures in the presented hybrid topology in a way that the diameter of the hybrid topology becomes comparable to the diameter of the star topology. In fact, it is equal to the diameter of the star topology plus 2. The proposed hybrid topology takes the shape of an  $n$ -star, and a remarkable improvement of data lookup latency with message complexity of  $O(n)$  is achieved, where  $n$  is the number of group heads, and  $n$  is usually very small compared to the total number of peers in the network.

**Key Words:** Residue Class, Interest-based, P2P Network, Star Interconnection Network, Diameter, Unicast Query, Lookup Latency.

Peer-to-peer (P2P) overlay networks are widely used in distributed systems due to their ability to provide computational and data resource sharing capability in a scalable, self-organizing, distributed manner. There are two classes of P2P networks: unstructured and structured ones. In unstructured systems [1] peers are organized into arbitrary topology. It takes help of flooding for data look up. Problem arising due to frequent peer joining and leaving the system, also known as churn, is handled effectively in unstructured systems. However, it compromises with the efficiency of data query and the much-needed flexibility. Besides, in unstructured networks, lookups are not guaranteed. On the other hand, structured overlay networks provide deterministic bounds on data sequential discovery. They provide scalable network overlays based on a distributed data structure which actually supports the deterministic behavior for data lookup. Recent trend in designing structured overlay architectures is the use of distributed hash tables (DHTs) [2]-[4]. Such overlay architectures can offer efficient, flexible, and robust service [2]-[6]. However, maintaining DHTs is a complex task and needs substantial amount of effort to handle the problem of churn. So, the major challenge facing such architectures is how to reduce this amount of effort while still providing an efficient data query service. In this direction, there exist several important works, which have considered designing DHT-based hybrid systems [17]-[21]; these works attempt to include the advantages of both structured and unstructured architectures. However, these works have their own pros and cons. Another design approach has attracted much attention; it is non-DHT based structured approach [27]. It offers advantages of DHT-based systems, while it attempts to reduce the complexity involved in churn handling.

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There exists yet another important approach; it is interest-based P2P networks. It is a structured approach without using DHT. Therefore, it does not have the problems that DHT based architecture faces, while at the same time it supports the deterministic behavior for data lookup. There exist several works in the literature in this direction [7]-[10], [14]-[16], [22]-[26].

It is an interest-based system. Two of the most prominent advantages relevant to the present work are: (1) all peers with the same interest (or possessing same resource type) structurally form a group of diameter one, and (2) the group heads are connected in the form of a ring and the ring always remains connected even in presence of any churn. These two advantages help in designing a very efficient data look-up algorithm [10]. However, we observe that there is scope to improve further the latency of the data look-up algorithm; all that is required for this purpose is to reduce the diameter of the ring, because this latency is dependent on the diameter ( $k/2$ ) of the ring (with  $k$  group heads). As  $k$  increases, latency of the existing look up algorithm increases as well. We observe that a star topology with same number of nodes (group heads) has much smaller diameter compared to the RC based architecture. Therefore, to reduce the diameter further the work reported in [13] has suggested the possibility of designing a hybrid architecture that combines the structural advantages of both RC-based and star-based topologies [11]. Objective is to reduce data lookup latency which reduces as diameter reduces. Therefore, in this paper, we have considered designing a hybrid architecture consisting of RC-based ones and Star topology; we name this architecture as hybrid star architecture. We have identified several important architectural properties of Star topology and have used them to design an efficient low latency unicast query propagation algorithm suitable for the hybrid architecture. We have made sure that the diameter of the redesigned RC based hybrid architecture which takes the shape of a star network (say  $n$ -star) is comparable with that of a non-hybrid  $n$ -star network with the same number of nodes (group heads), thereby ensuring remarkable improvement of the data look-up latency. In the worst-case, the total number of message transmissions is only  $(2n-3)$  for an  $n$ -star hybrid network. In this work, we shall use the words, architecture and topology, interchangeably.

## 2 RC Based Topology and Star Topology

We first state briefly the architecture of RC based network followed STAR topology.

### 2.1 RC Based architecture [10]

**Definition 1:** We define a resource as a tuple  $\langle R_i, V \rangle$ , where  $R_i$  denotes the type of a resource and  $V$  is the value of the resource. A resource can have many values. For example, let  $R_i$  denote the resource type 'movies' and  $V'$  denote a particular actor. Thus  $\langle R_i, V' \rangle$  represents movies (some or all) acted by a particular actor  $V'$ .

**Definition 2:** Let  $S$  be the set of all peers in a peer-to-peer system. Then  $S = \{PR_i\}$ , where  $0 \leq i \leq n-1$ , and  $PR_i$  denotes the subset consisting of all peers with the same resource type  $R_i$ . The number of distinct resource types present in the system is  $n$ . Also, for each subset  $PR_i$ , we assume that  $P_i$  is the first peer among the peers in  $PR_i$  to join the system. We call  $P_i$  the group-head of group  $G_i$ , which is formed by the peers in the subset  $PR_i$ .

#### A. Two level P2P architecture

It is a two-level overlay architecture and at each level structured networks of peers exist. It is explained below.

1. At level-1, we have a ring network consisting of the peers  $P_i$  where  $0 \leq i \leq n-1$ . The number of peers (i.e., group heads) on the ring is  $n$ , which is also the number of distinct resource types. This ring network is used for efficient data lookup and is named the transit ring network.

2. At level-2, there are  $n$  completely connected networks (groups) of peers. Each such group, say  $G_i$ , is formed by the peers of the subset  $PR_i$ , where  $0 \leq i \leq n-1$ , such that all peers  $\in PR_i$  are directly connected (logically) to each other, resulting in a network diameter of 1. Each  $G_i$  is connected to the transit ring network via its group-head  $P_i$ .

3. Any communication between a peer  $p'_i \in G_i$  and  $p'_j \in G_j$  takes place only via the respective group-heads  $P_i$  and  $P_j$ .

The architecture is shown in Figure 1.

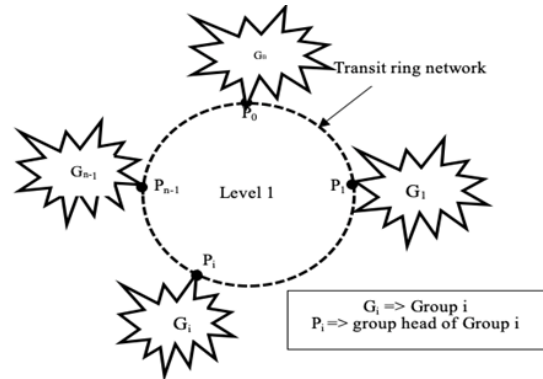


Figure 1: An RC-based P2P network

#### B. Assignments of overlay addresses

Consider the set  $S_n$  of nonnegative integers less than  $n$ , given as  $S_n = \{0, 1, 2, \dots, n-1\}$ . This is referred to as the set of residues, or residue classes (mod  $n$ ). That is, each integer in  $S_n$  represents a residue class (RC). These residue classes can be labeled as  $[0], [1], [2], \dots, [n-1]$ , where

$$[r] = \{a : a \text{ is an integer, } a \equiv r \pmod{n}\}.$$

For example, for  $n = 3$ , the classes are:

$$[0] = \dots, 6, 3, 0, 3, 6, \dots$$

$$[1] = \dots, 5, 2, 1, 4, 7, \dots$$

$$[2] = \dots, 4, 1, 2, 5, 8, \dots$$

A relevant property of residue class is stated below.

**Lemma 1.** Any two numbers of any class  $r$  of  $S_n$  are mutually congruent. Assume that in an interest-based P2P system there are  $n$  distinct resource types. Consider the set of all peers in the system given as  $S = \{PR_i\}$ , where  $0 \leq i \leq n-1$ . Also, as mentioned earlier, for each subset  $PR_i$  (i.e., group  $G_i$ ), peer  $P_i$  is the first peer with resource type  $R_i$  to join the system.

In this overlay architecture, the positive numbers belonging to different classes are used to define the following parameters:

1. Logical addresses of peers in a subnet  $PR_i$  (i.e., group  $G_i$ ). The use of these addresses has been shown to justify that all peers in  $G_i$  are directly connected to each other (logically), forming an overlay network of diameter 1. In graph theoretic terms, each  $G_i$  is a complete graph.

2. Identifying peers that are neighbors to each other on the transit ring network.

3. Identifying each distinct resource type with unique code.

The assignment of logical addresses to the peers at the two levels and the resources happen as follows:

At level-1, each group-head  $P_r$  of group  $G_r$  is assigned the minimum nonnegative number  $r$  of residue class  $r \pmod{n}$  of the residue system  $S_n$ .

At level-2, all peers having the same resource type  $R_r$  will form the group  $G_r$  (i.e., the subset  $P_{R_r}$ ) with the group-head  $P_r$  connected to the transit ring network. Each new peer joining group  $G_r$  is given the group membership address  $r + j \cdot n$ , for  $j = 1, 2, \dots$

3. Resource type  $R_r$  possessed by peers in  $G_r$  is assigned the code  $r$  which is also the logical address of the group-head  $P_r$  of group  $G_r$ .

4. Each time a new group-head joins, a corresponding tuple  $\langle \text{Resource Type, Resource Code, Group Head Logical Address} \rangle$  is entered in the global resource table (GRT).

**Definition 3.** Two peers  $P_i$  and  $P_j$  on the ring network are logically linked together if  $(i + 1) \pmod{n} = j$ . Remark 2. The last group-head  $P_{n-1}$  and the first group-head  $P_0$  are neighbors based on Definition 3. It justifies that the transit network is a ring.

**Definition 4.** Two peers of a group  $G_r$  are logically linked together if their assigned logical addresses are mutually congruent.

**Lemma 2.** Diameter of the transit ring network is  $n/2$ .

**Lemma 3.** Each group  $G_r$  forms a complete graph.

## 2.2 STAR Architecture [11]

The address of a node in an  $n$ -star  $S_n$  is identified by a unique permutation of the digits  $\{1, 2, 3, \dots, n\}$ . Let  $f_i$ , ( $2 \leq i \leq n-1$ ) be a function that maps permutation  $P_k$  of the digits  $1, 2, 3, \dots, n$  to another permutation  $P'_k$ , i.e.  $f_i(P_k) = P'_k$  where the first and the  $i^{\text{th}}$  digits in  $P_k$  are interchanged to generate  $P'_k$ .

The mapping function  $f_1$  on  $P_k$  is such that the first and the  $n$ th digits in  $P_k$  are interchanged to generate  $P_m$ . That is,  $f_1(P_k) = P_m$ . In other words, the last digit of  $P_m$  is identical to the first digit of  $P_k$  and vice-versa; meaning thereby that  $P_k$  and  $P_m$  belong to two different  $S_{n-1}$  stars which are the components of  $S_n$  and the nodes represented by these addresses, i.e.,  $P_k$  and  $P_m$  are directly connected to each other. For example, in a 4-star, any two of the component 3-stars have two links connecting them. Thus, we see that number of nodes in a complete  $n$ -star is  $n!$

An example of a complete 4-star,  $S_4$  is shown in Figure 2. Note that it has 24 (4!) nodes and each component 3-star,  $S_3$  is also a complete one and has 6 (3!) nodes. That is, the  $S_4$  has four component complete 3-stars. However, in general, a star may be an incomplete one as well. Later when we use the topological properties of a star to design the modified RC based network, a node in a star means a group head as in the RC based one.

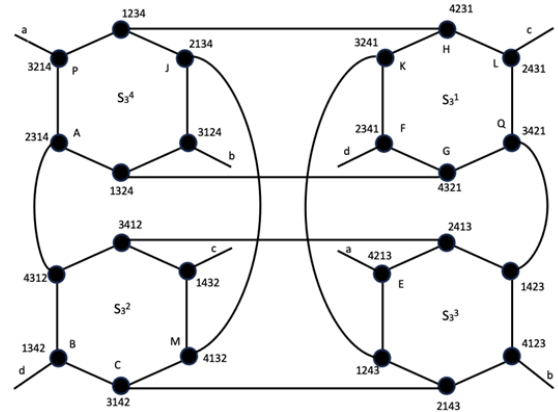


Figure 2: A complete 4-star architecture

2.3 Comparison of the diameters of the two architectures  
We shall consider number of overlay hops between nodes as the parameter to determine diameters. For this purpose, in RC based one, we consider only the group heads located on the ring. The peers inside a group form a network of diameter 1 and so, we may not need to count it while determining the diameter of the (transit) ring because a group head may not have any other member present at a given time. For Star architecture [11] we consider only the nodes that form the architecture. Later in this paper, we shall propose a hybrid star topology using both RC-based ones and star networks in which a node represents a group head of peers with identical interest. The comparison of diameters of RC-based networks and star interconnection networks is stated below.

From the information stated above, we observe that as the number of group heads/nodes increases, diameter of RC based architecture increases much faster compared to the diameter of a star architecture. Therefore, latency of any data look-up protocol will be much smaller in a Star network compared to that in an RC based network.

RC-based ring network		Star interconnection network		
Number of Group heads	Diameter	Complete Star	Number of nodes	Diameter
6	3	3-Star	6	3
24	12	4-Star	24	5
120	60	5-Star	120	7
720	360	6-Star	720	9

Table 1: Comparison of RC-based ring network and Star interconnection network

### 3 A Six-node Basic RC Component and A Complete 3-Star

We highlight below the similarities and dissimilarities between a six-node basic RC-based component and a complete 3-Star.

Let us consider the two architectures as shown in Figure 3 and Figure 4. We name the first one as a basic RC-based component. The second one shows a complete 3-star. One main reason to consider such an RC based component is that it is very unlikely that there will exist less than six distinct types of resources at any time. Even if it is, as will be clear later that (see Section 4, Figure 5 and Figure 6) the architecture will simply be an RC-based ring with less than six nodes. The structural similarities and dissimilarities of the two architectures are stated below. As is seen in the figures, the overlay addresses in the two architectures are based on RC based idea and star-based idea respectively. The two architectures have the same diameter (3 in terms of hop). So, data look-up latency in both can be at most 3. This is the similarity. Now, consider that node f has left. In Figure 3, the topology remains connected, i.e., it remains a ring [10]. So, performance of any data look-up protocol does not degrade. However, in Figure 4, the same is not true because the topology is a disconnected one resulting in an incomplete 3-star. This is the dissimilarity. This simple and yet important observation will be used in constructing the proposed architecture.

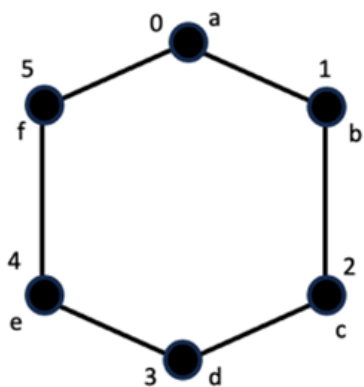


Figure 3: RC-based component

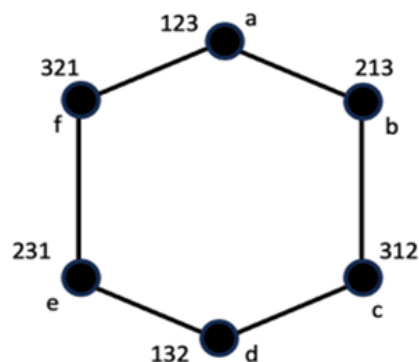


Figure 4: A complete 3-star

### 4 The Proposed Hybrid Architecture and Some Relevant Properties

In the proposed architecture we assume that it will consist of a number of basic RC-based components and the components will be connected to form a complete n-star. Data look-up inside an RC-based component will follow the existing data look-up protocol reported in [10] using the RC-based overlay addresses of the nodes and inter-component routing (i.e., to send any query from component to component) will use the star-based overlay addresses. Note that in the architecture, every node in the star will be a group-head of peers with the same resource type. We shall use group-head and node interchangeably. The reason for consideration of such intra-component and inter-component query protocols is two-fold: 1) under no circumstances an RC-based component can be disconnected, so there will be no degradation of performance of the look-up process, and the latency of intra-component query look-up will be limited by 3 hops, 2) overlay distance between any two nodes in the hybrid architecture will at most be equal to the diameter of the n-star plus 2; this 2 is due to the fact that diameter of each source group and destination group is 1. Therefore, it results in a much less latency required for the query propagation compared to that in an RC based ring topology with the same number of nodes n!.

In the above architectural design, a node needs to have a tuple of overlay addresses (a1, a2), in which a1 represents the node's RC-based overlay address and a2 represents its star-based overlay address. For example, in Figure 3, the address tuple of node 'a' will now become (0, 123). The first one is used for intra-component query propagation and the second one

is used for the inter-component query propagation.

We now illustrate briefly how the proposed architecture is constructed. Let us start with a single node 'a'. The address tuple of the node 'a' is (0, 123). Now consider that a second node 'b' joins (Figure 5). The address of this second node is (1, 213). Note that it is now a ring of two nodes (see the dotted link between the two nodes). Now consider that a third node 'c' joins. Its address tuple is (2, 312). The basic component structure is still a ring (see the dotted link in Figure 6). However, if we consider a 3-star with these three nodes, it is just incomplete and definitely the performance of any query in it will degrade. This will go on unless the component contains all six nodes. This is the reason which we mentioned earlier, why each component will be constructed using RC based idea. However, when a new node, say 'g', (seventh one) joins, it will form the second basic component (of a 4-star) with one node only and the overlay address tuple of 'g' will be 4231 while at the same time the second component address of each of the nodes in the first basic component will be updated as xxx4 (see Section 2.2). In addition, based on star topology, node 'a' and node 'g' will have a direct overlay link for inter-component query propagation. The structure is shown in Figure 7. In this way, using RC based components, star topologies of higher dimensions can be constructed. In this context, it may be mentioned that while the number of the distinct resource types is limited [12], the number of members in a group can be enormously large (theoretically infinite). This is one of the main characteristics (advantages) of the residue class-based design and it has been incorporated in the Star architecture (of the proposed design) consisting of basic RC Based components.

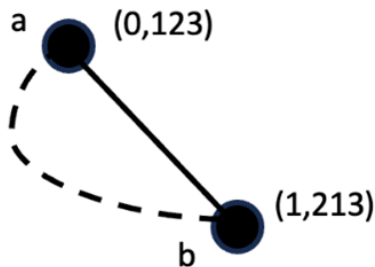


Figure 5: A two-node component

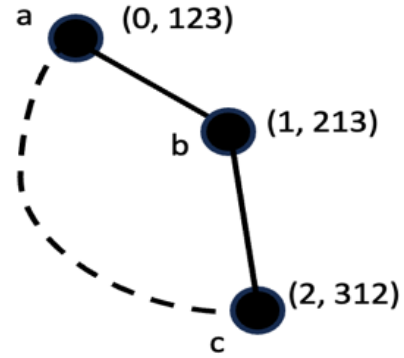


Figure 6: A three-node component

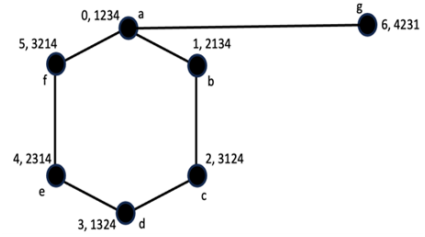


Figure 7: An incomplete 4-star

Note that in general, for an n-star, the star-based overlay address of any node will be a specific permutation of the n literals, viz., 1,2,3,...,n.

We now define 'neighbors' of a node x in a basic RC-based component using its star-based overlay address. Let this address be ABC. Then, nodes with addresses BAC and CBA are the neighbors of node x. It means that node x has direct logical connections with these two nodes in the basic component which is also a complete 3-star. These connections can be used by node x for intra-basic component or simply intra-component routing. Now assume that the overlay topology appears as a complete 4-star. So, we now add another literal, say D in the overlay address of node x and the address becomes ABCD. Then, according to star topology node x will be logically connected to node DBCA that belongs to a different 3-star. Therefore, degree on node x increases from 2 in a basic component to 3 in 4-star topology. Thus, node x has three neighbors in 4-star topology. This connection to the 3rd neighbor implies that node x can use this for inter-component routing in the 4-star. Now consider that this 4-star is a part of a complete 5-star. Then, the address of x will consist of 5 literals and so it becomes ABCDE. Then, according to 5-star topology node x will be logically connected to node EBCDA. Therefore, node x now has 4 neighbors. To conclude, in an n-star overlay hybrid architecture, degree of any node is (n-1). Thus, any node can use these addresses (of neighbors) to multicast its information to different basic components of the topology. This idea may be used to incorporate parallelism in broadcasting by any node in the network. In this context, it is understood that the overlay address (be it basic RC-based component or not) of a node will be paired with its IP address.

Example:

In Fig 4, node with address 123 has its neighbors as 213 and 321.

In Fig. 2, the 4-star address of the above node will have 4 literals and it is 1234. Neighbors of the node with 4-star based overlay address 1234 are 2134, 3214, and 4231. The first two are in the same RC-based component as is the node 1234, and the 3rd one is in another RC-based component in the parent 4-star. We name this 3rd one as an inter-component neighbor of the node 1234. For inter component propagation of query/data from node 1234 to node 4231, and vice-versa, this 3rd neighbor is necessary. Note that the 3rd one is obtained by interchanging the first and the 4th literals of 1234.

If it is a 5-star, address of the above node will have 5 literals and it is 12345; its 4 neighbors are 21345, 32145, 42315, and 52341. The first two are in the same RC-based component as is the node 12345. In this case, the 3rd and 4th nodes are the inter-component neighbors of node 12345. The 3rd one is used for propagation of information from node 12345 to a different RC-based component belonging to the same parent 4-star. The 4th neighbor belongs to a different 4-star component of the 5-star topology and its address is obtained by interchanging the first and the 5th literals of 12345; it is used for information propagation between two 4-stars.

In general, a node in an n-star will have (n-1) different neighbors; two of them belong to its parent RC-based component and the rest are one for each higher order star respectively. It may be noted that the n-star is a nested architecture in a sense that it consists of (n-1) stars; each (n-1) star consists of (n-2) stars and so on till it comes down to component 3-stars.

For low latency propagation (limited by the diameter of a given star topology) we consider that the following information to be present with each node in an n-star. Each node maintains the following tables:

- 1) Resource table for basic component (RT-Basic)
- 2) Resource tables for next higher order stars (RT-4-Star, RT-5-Star, etc.)
- 3) Each node maintains a list of its (n-1) neighbors.

Example:

Consider the RC-based component and the 3-star of Figures 3 and 4. The RT-Basic for the nodes in a basic component appears as

Table 2: RT-basic

nodes	resource-code (ar)	3-star-based address (as)
a	0	123
b	1	213
c	2	312
d	3	132
e	4	231
f	5	321

In the above table, RT-based overlay address of a node and the resource code it possesses are the same ones.

Table for the 4-star of Fig. 2 is shown below:

Table 3: RT-4-Star

resource-code-range	4-star-based-address-range
0, 5	xxx4
6, 11	xxx2
12, 17	xxx1
18, 23	xxx3

In this table, each row corresponds uniquely to one 3-star component of a 4-star. In a row, the first entry denotes the lower and the upper code values of the six resources present uniquely with the six nodes belonging to a component 3-star; the second entry denotes that the star-based overlay addresses of the six nodes in it end with the same literal. Note that overlay addresses of the six nodes can be obtained by permutations of the first three literals (denoted as xxx) while the 4th literal is fixed in all these six addresses.

Table 4: RT-5-Star

resource-code-range	5-star-based-address-range
0, 23	xxxx5
24, 47	xxxx2
48, 71	xxxx3
72, 95	xxxx4
96, 119	xxxx1

In this table for a 5-star, each row corresponds uniquely to one 4-star component of a complete 5-star. The corresponding 5-star topology is not shown here; however, the above table actually gives the information of the topology. In a row, the first entry denotes the ranges of resources (resource codes) present in the component, and the second entry denotes that the overlay addresses of the 24 nodes in it end with the same literal. Therefore, we observe that for an i-star topology, it will have i numbers of component (i-1) stars. We denote a component as the  $m'h$  component in which the  $i'h$  literals in the overlay addresses of all nodes in the component are m. For example, in the above RT-5-star table, there are five 4-star components, and the respective  $5'h$  literals in the overlay addresses of the five component 4-stars are 1, 2, 3, 4, and 5. That is, all nodes in component one will have 1 as the last literal in their overlay addresses; all nodes in component two will have 2 as the last literals in their overlay addresses; and so on.

In a similar way as above, tables can be built for higher order stars. However, it has been shown that in reality the number of distinct resource types is limited [12].

Therefore, we suggest that the design consideration should be restricted to a maximum of 6-star that contains 720 distinct resource types (Section 2.3). If necessary, a federation of 6-stars or even of 5-stars can be built (not covered in this paper). However, the proposed unicast algorithm in Section 5 is a

general one that considers any hybrid n-star topology. In this context, we repeat that each node is the group-head of a group of peers possessing similar kind of resources, and the construction of each group is such that it can contain very large number of such peers (theoretically infinite). Note that for an n-star hybrid topology, the total number of rows of the tables together is  $(6+4+5+6+\dots+n)$ , i.e.,  $n(n+1)/2$ . Thus, for a 6-star topology, it will be  $21 \times 2$  only, which is reasonably quite small for any group-head (node) to store.

## 5 Data Look-up Algorithm.

Let us present an algorithm for unicast communication. We assume that in an n-star hybrid topology a query for an instance of a resource with code  $ar'$  is originated at a node with a tuple of overlay addresses  $(ar, as)$ . Each node maintains tables such as its parent RT-basic, RT- 4-star, RT-5-star, and so on. Each node maintains a list of its neighbors.

### 5.1 Algorithm Unicast

We start with a description of searching inside a RC-based component as this will be used in the main body of the unicast algorithm as a subroutine.

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#### Algorithm 1 Intra-RC-Based-Component

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if  $ar' \in RT\text{-basic}$  [ $ar - ar'$ ] > 3
  Diameter of a RT-based component is 3  $ar$  forwards the
  query to its immediate predecessor
else
   $ar$  forwards the query to its immediate successor
for each intermediate receiving node  $N$ 
   $N$  forwards the query until its code is equal to  $ar'$ 
if  $N$  has the answer to the query  $N$  unicasts the answer to
  node  $ar$  using the IP address of  $ar$ 
else
  One-hop communication since the diameter of each group-
  head is one  $N$  broadcasts the query in its group-heads
if  $\exists p'$  with  $ar'$ 
  Peer  $p'$  unicasts  $ar'$  to  $ar$ 
else
  Search latency in the group-heads is minimal, i.e., only two
  hops Search latency in the group-heads is minimal, i.e.,
  only two hops

else
  Execute Algorithm Unicast

```

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#### Algorithm Unicast:

1. The originator node, identified by the tuple of overlay addresses  $(ar, as)$ , starts searching through the resource tables of higher-order stars. The search continues until a

resource with the code  $ar'$  is found in some  $m^{th}$  component of an  $(i-1)$ -star of an  $i$ -star, where  $4 \leq i \leq n$ . Since the originator node belongs to a 3-star component, the search begins with its parent 4-star. The search then continues through progressively higher-order stars until the desired resource is located.

2. Node  $ar$  finds the  $i$ th literal, i.e.,  $m$ , in the  $n$ -star-based overlay address of the  $m$ th component of the  $(i-1)$ -star.
3. If node  $ar'$ 's overlay address starts with the literal  $m$ , node  $ar$  interchanges the first literal with the  $i$ th literal of its address. Node  $ar$  then forwards the query to the node with this modified address in the  $m$ th component of the  $(i-1)$ -star, and control flows to step 7.
4. Node  $ar$  finds its neighbor whose overlay address starts with the literal  $m$ . Each node in a 3-star component has exactly one neighbor in each higher-order star.
5. Node  $ar$  forwards the query to the neighbor.

6. neighbor node interchanges the first literal with the  $i$ th literal of its address and forwards the query to the node with this address in the  $m$ th component  $(i-1)$ -star.

/ receiving node is an inter-component neighbor of the sending node

7. receiving node in the  $m$ th  $(i-1)$ -star now becomes the new originator node and the following steps 7.1, 7.2 are executed.

7.1. new originator node searches its resource table to identify the  $(i-2)$ -star that has the resource; steps 2 to 6 are executed with this new originator and the  $(i-2)$ -star; this process continues until a 3-star is identified to have the resource

/ Resource tables of lower order stars from  $(i-2)$ -star to 4-star are searched

7.2 control flows to Algorithm Intra-RC-Based-Component

**Theorem 1.** Message complexity of Algorithm Unicast is  $O(n)$ .

**Proof.** Proof is constructive. Worst-case appears when in Step 1 of Algorithm Unicast implies that if the resource is initially found in some component  $(n-1)$ -star of the n-star hybrid topology, steps 2 to 7.1 will be executed repeatedly until a 3-star is identified to have the resource. During each repetition, the query is sent to an appropriate node in a star of immediate lower dimension. Thus, so far  $(n-3)$  message-transmissions take place. Once in a 3-star it takes at most 3 overlay hops (diameter of a 3-star can be at most 3) to reach the final probable destination. So, all together there are  $[(n-3) + 3] = n$  message-transmissions. However, if Steps 4 and 5 are to be executed in each repetition,  $(n-3)$  more message transmissions take place. Therefore, total number of message transmissions in the worst-case is  $n+(n-3)$ , i.e.  $(2n-3)$ . Hence, the message complexity is  $O(n)$ .

#### Example of unicast query propagation

Let us consider the 4-star network of Fig. 2. Let a peer in group  $j$  with group-head address tuple  $(1, 2134)$  has requested its group-head for a particular instance of a resource with resource

code 11. Note that the group-head may itself be the requesting peer. Let us denote this group-head as  $g_j$ . Group-head  $g_j$  maintains its tables RT-basic and RT-4-star. It first searches the table RT-basic and does not find the resource 11 in it. It then searches the table RT-4-star, and the 3rd entry (12, 17 xxx1) indicates that resources with codes from 12 to 17 exist with the peers of the RC-based component 3-star in which the 4-star based addresses of all six nodes end with the literal 1. Now  $g_j$  finds its neighbor that has its overlay address starting with the literal 1 and it is 1234. Node  $g_j$  sends the query to the neighbor 1234.

Node 1234 interchanges the first literal with the 4th literal of its address to obtain 4231 and sends the query to this new node 4231. If node 4231 possesses resource with code 11 and if has the answer to the query, it directly sends the reply to the requesting group-head  $g_j$ ; else it broadcasts the query in its group to learn if a peer in its group has the answer. If so, the peer sends the answer to  $g_j$  directly; otherwise search fails. On the other hand, if node 4231 has different resource code, it then initiates the searching in its parent RT-based component 3-star. This searching to identify the group-head that owns the resource code 11 takes at most 3 overlay hops as the diameter of any RC-based component can be at most 3. Searching for the correct group-head can also be done without any propagation of the query in the basic component. It can be done by node 4231 via a simple search of the appropriate RT-basic table for the correct owner of the resource with code 11. Node 4231 then has to contact the owner directly informing about the query. However, because of very low diameter of a basic component, query propagation may be a reasonably good idea and therefore, in this work, we have considered the query propagation approach. Finally, as stated above if a peer (be it a peer in a group or a group-head itself) is found to have the answer, it will directly send the answer to the requesting group-head.

## 5.2 Fault Tolerance

Observe that links in a star topology are physical [11] while in our proposed hybrid architecture using both RC-based and star topology, links are virtual. Hence, there is no need to consider any link failure.

In addition, each node here is actually the group-head of a group of peers with similar kind of resources (interests) and the construction of each group is such that it can contain very large number of such peers (theoretically infinite); therefore, it is very unlikely that a complete group of peers will disappear because of churn [10]. It may be noted that inclusion or exclusion (leaving) of any peer, related to an existing group does not change the diameter of the group (which is one); since peers in a group form a complete graph.

## 6 Conclusion

In this work we have used some topological properties of Star inter-connection networks to redesign an already existing

Residue class-based peer-to-peer architecture. The existing RC-based architecture has been the choice in this work because of its manifold advantages. Specifically, the following two structural properties are behind the choice: these are (1) all peers with the same interest (or possessing same resource type) structurally form a group of diameter one, and (2) the group heads are connected in the form of a ring and the ring always remains connected even in presence of any churn. However, data look-up latency is  $k/2$  for an RC-based network with  $k$  group heads. It may appear substantial if  $k$  is large. In order to reduce this latency, some pertinent topological properties of Star network have been used to modify the existing RC based design. The proposed hybrid design has much less diameter than in its original design (RC based design). It reduces the data look-up latency remarkably. In an  $n$ -star hybrid topology, the overlay distance between any two nodes in the hybrid architecture will at most be equal to the diameter of the  $n$ -star network plus 2; this 2 is due to the fact that diameter of each source group and destination group is 1. Therefore, it results in a much less latency required for the query propagation compared to that in an RC based ring topology consisting of the same number of nodes  $n!$  as in the  $n$ -star hybrid network.

Future works aim at designing secured multicast and broadcast data look-up algorithms in the proposed design.

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